

# Taxing Entrepreneurs and Workers

*A Linear Optimization Approach for Multidimensional Screening*

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# Introduction

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Large share of high income are entrepreneurs: how should we design redistributive taxation?

- ▶ Mirrlees model ill-suited to answer this question: only considers workers with fixed wage.
- ▶ Ideally: GE model w/ two-dimensional ability (worker, entrepreneur) & occupational choice.

Major technical issue: multidimensional screening problem!

- ▶ With two-dim private info, the structure of binding incentive constraints is intractable.
- ▶ Most of the literature ends up assuming or ensuring that only local IC constraints bind.

This paper: we solve the full multidimensional mechanism design problem numerically.

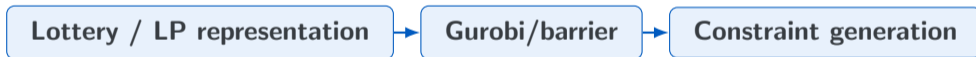
- ▶ Impose *all* (global) IC constraints in a non-convex environment (fixed costs).

# A Numerical Approach to Solving Multidimensional Screening Problems

Starting point: recast the problem as a linear program over lotteries.

- ▶ Well-established theory developed by Prescott-Townsend 1984, Doepke-Townsend 2006.
- ▶ Curse of dimensionality: requires introducing large number of constraints and controls.

We leverage modern large-scale linear programming (LP) solvers.



This approach is applicable more broadly than to the specific economic problem we're studying!

- ▶ Key advantage: method can handle *arbitrary* non-convexities and non-differentiabilities.

## This paper

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We study optimal taxation when agents privately types are two-dimensional and choose between work and entrepreneurship.

- ▶ **Environment.** Agents differ in labor skill  $s$  and entrepreneurial ability  $z$ ; wage work is riskless, entrepreneurs face idiosyncratic productivity risk.
- ▶ **Policy.** The government observes labor income  $y$  and realized dividends  $d$ , so feasible taxes are  $T(y, d)$ .
- ▶ **Solution.** We solve a lottery-based linear formulation of the planner's problem, with *all* (global) IC constraints.

# Main result

## Key takeaway

Optimal policies create tax breaks, or subsidies, for types near the occupational choice frontier, where non-local IC constraints bind.

- ▶ High-skill workers have attractive labor outside options.
- ▶ Some of them are also good potential entrepreneurs.
- ▶ To induce entry into entrepreneurship, the planner grants information rents near the occupational frontier.

## General equilibrium amplification

With decreasing returns, no single firm can absorb the entire labor supply. The economy needs enough entrepreneurial entry to generate sufficient labor demand.

## Related Literature

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- ▶ **Multidimensional Screening:** Armstrong (1996), Rochet (1998), Manelli & Vincent (2007); recent public finance applications: Kleven et al. (2009), Scheuer (2014), Rothschild & Scheuer (2013), Golosov et al. (2025), Shen et al. (2025).
- ▶ **Global Incentive Compatibility:** Lottery-based LP (Prescott Townsend 1984, Phelan Townsend 1991, Doepke Townsend 2006) + constraint generation + modern solvers (Gurobi/CPLEX).
- ▶ **Alternative LP Approaches:** Rochet (2024); Carlier et al. (2024); Boerma, Tsyvinski & Zimin (2022): we allow for non-convex, non-smooth primitives.
- ▶ **Optimal taxation of entrepreneurs:** Scheuer (2014).

## Model

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## Model: heterogeneity and choices

A unit mass of agents, each with privately known type

$$(s, z) \in \mathcal{S} \times \mathcal{Z}$$

- ▶  $s$ : labor skill.
- ▶  $z$ : entrepreneurial ability.
- ▶ Joint distribution  $f(s, z)$ ; quantitative model uses Fréchet marginals and a copula.

Before entrepreneurial shocks are realized, each agent chooses one occupation:

Worker

Entrepreneur

Inactive

### Exclusive occupations:

workers supply effort  $\ell$ , entrepreneurs choose effort  $e$  and hire labor  $n$ , inactive agents consume home production  $c_0$ .

## Model: observables

The government observes realized labor income and realized entrepreneurial dividends.

$$\text{Worker: } y = w \cdot s \cdot \ell - \kappa_1 \cdot \mathbf{1}[\ell > 0]$$

$$\text{Entrepreneur: } q = z \cdot \varepsilon \cdot e^\alpha \cdot n^{1-\alpha}$$

$$d = q - w \cdot n - \kappa_2 \cdot \mathbf{1}[n > 0]$$

### What is hidden?

The planner does not observe  $(s, z)$ , effort, labor demand, or the shock  $\varepsilon$  separately.

$$y > 0 \Rightarrow d = 0, \quad d > 0 \Rightarrow y = 0.$$

## Model: incentive constraints

A direct mechanism assigns observable outcomes and consumption as a function of reported type.

For every true type  $(s, z)$  and every report  $(\hat{s}, \hat{z})$ , truthful reporting must dominate the deviation:

$$\begin{aligned} & \mathbb{E}_\varepsilon[U(c(s, z, \varepsilon)) - V(e(s, z, \varepsilon)) - V(\ell(s, z))] \\ & \geq \mathbb{E}_\varepsilon[U(c(\hat{s}, \hat{z}, \varepsilon)) - V(e(\hat{s}, \hat{z}, \varepsilon; z)) - V(\ell(\hat{s}, \hat{z}; s))] . \end{aligned}$$

### Why global IC matters

Not all tempting deviations are local. Non-local incentive constraint can bind near occupational switching regions.

## Model: general equilibrium

The planner must also respect aggregate feasibility and labor-market clearing.

$$\int \mathbb{E}_\varepsilon[c(s, z, \varepsilon)]f(s, z) ds dz \leq \int \mathbb{E}_\varepsilon[y(s, z) + d(s, z, \varepsilon)]f(s, z) ds dz,$$
$$\int sl(s, z)f(s, z) ds dz = \int \mathbb{E}_\varepsilon[n(s, z, \varepsilon)]f(s, z) ds dz.$$

### Key GE force

Taxes affect entry and firm scale. Entry affects labor demand. Labor demand affects wages and aggregate income.

# Why the problem is hard

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Four features make standard local methods fragile:

1. **Two-dimensional private information:** reports are pairs  $(\hat{s}, \hat{z})$ .
2. **Occupational non-convexities:** worker, entrepreneur, and inactive choices are discrete.
3. **Fixed costs:**  $\kappa_1$  and  $\kappa_2$  create kinks.
4. **Risk-contingent observables:** dividends are affected by shocks, which are not observed directly.

## Solution strategy

Discretize types, shocks, and feasible allocations. Optimize over lotteries on this grid. Enforce all relevant IC constraints with constraint generation algorithms.

# Lottery Representation

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## LP grid: what are the controls?

Discretize types, shocks, and allocation nodes.

$$i = 1, \dots, N, \quad r = 1, \dots, R,$$
$$C = \{c_k\}_{k=1}^K, \quad Y = \{\bar{y}_a\}_{a=1}^{A_y}, \quad D = \{\bar{d}_b\}_{b=1}^{B_d}.$$

Admissible income-dividend pairs satisfy occupational exclusivity:

$$\mathcal{J} = \{(a, b) : \bar{y}_a > 0 \Rightarrow \bar{d}_b = 0, \bar{d}_b > 0 \Rightarrow \bar{y}_a = 0\}.$$

### Linear representation

For each reported type and shock, the LP chooses probabilities over consumption nodes and income-dividend nodes. These probabilities are the controls. For a fixed grid, expected utility, resources, labor demand, and IC expressions are all linear in lottery weights.

## A simple example of the LP expansion

Assume two labor-income nodes, two dividend nodes, and two consumption nodes:

$$Y = \{0, y\}, \quad D = \{0, d\}, \quad C = \{c_L, c_H\}.$$

Exclusivity removes the mixed point  $(y, d)$ , so

$$\mathcal{J} = \{(0, 0), (y, 0), (0, d)\}.$$

For each type and shock, the LP can mix over

2 consumption nodes + 3 occupation/outcome nodes.

### Takeaway

A small economic menu induces many controls variable once we allow lotteries over consumption, occupations, dividends, and shock-contingent outcomes.

## Sketch of the LP representation

For each type  $i$ , expected utility at truth-telling is

$$EU_i = \sum_r p_r \left[ \sum_k \lambda_{i,k,r} U(c_k) - \sum_{(a,b) \in \mathcal{J}} \mu_{i,a,b,r} \mathcal{V}_{i,a,b,r} \right]$$

The planner solves

$$\max_{\lambda, \mu} \sum_i \omega_i \cdot W_i \cdot EU_i$$

subject to simplex constraints, resource feasibility, labor-market clearing, participation, no shock-contingent occupation switching, and

$$EU_i \geq EU_{i \rightarrow j} \quad \forall i, j.$$

### Why this is powerful

The objective and all constraints are linear in  $(\lambda, \mu)$ . All nonlinearities are precomputed on the grid.

## Constraint counts

Let  $N = N_s \cdot N_z$  be the number of types,  $R$  the number of shock states,  $K$  consumption nodes, and  $|\mathcal{J}| = \underbrace{1}_{(0,0)} + \underbrace{(A_y - 1)}_{\text{worker nodes}} + \underbrace{(B_d - 1)}_{\text{entrepreneur nodes}}$  admissible income-dividend nodes.

Object	Lottery LP	Discretized nonlinear problem
Controls	$\underbrace{NRK}_{\lambda_{i,k,r}} + \underbrace{NR \mathcal{J} }_{\mu_{i,a,b,r}} = NR(K +  \mathcal{J} )$	$\underbrace{N}_{y_i} + \underbrace{NR}_{d_{ir}} + \underbrace{NR}_{c_{ir}} = N(1 + 2R)$
Global IC constraints	$N(N - 1)$	$N(N - 1)$
Participation constraints	$N$	$N$
Resource feasibility	$1$	$1$
Labor-market clearing	$1$	$1$
Simplex / consistency constraints	$2NR + NR[K +  \mathcal{J} ]$	$0$

### Computational tradeoff

The lottery representation makes the problem larger, but linear.

# Constraint counts and constraint generation

## Baseline grid

$$N = 60^2 = 3,600, \quad R = 2, \quad K = 50, \quad A_y = B_d = 30, \quad |\mathcal{J}| = A_y + B_d - 1 = 59.$$

	Lottery LP	Discretized nonlinear problem
Primitive controls	$\underbrace{NRK}_{\lambda} + \underbrace{NR \mathcal{J} }_{\mu} = 3,600 \cdot 2 \cdot (50 + 59) = 784,800$	$\underbrace{N}_{y_i} + \underbrace{NR}_{d_{ir}} + \underbrace{NR}_{c_{ir}} = 3,600(1 + 2R) = 18,000$
Global IC constraints	12,956,400 linear inequalities	12,956,400 nonlinear inequalities
Simplex constraints	14,400 equalities + 784,800 bounds	0

## Constraint generation

Rather than load all  $N(N - 1)$  global IC constraints, we solve a relaxed LP, search for violated deviations, add the most violated constraints, and iterate.

# Quantitative Analysis

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# Calibration: parameters

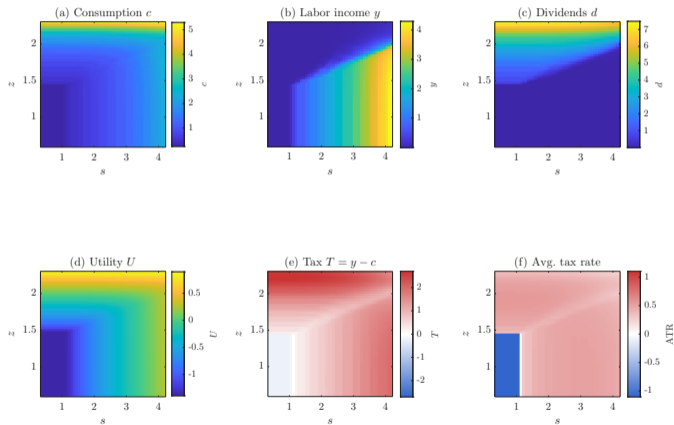
Parameter	Symbol	Value	Target moment	Source
<i>Set externally</i>				
Risk aversion	$\gamma$	1.00	Log utility	Standard
Inverse Frisch	$\psi$	2.00	Frisch = 0.5	Standard
Ability correlation	$\rho$	0.00	Independence	Standard
<i>Calibrated jointly</i>				
Worker fixed cost	$\kappa_1$	0.675	Labor participation	BLS (2022)
Entrep. fixed cost	$\kappa_2$	0.109	Entrepreneurship rate	BLS CPS (2022)
Span of control	$\alpha$	0.251	Avg. employees/firm	U.S. Census (2021)
Shock volatility	$\sigma_e$	0.500	CV of business income	<a href="#">DeBacker et al. (2021)</a>
Skill tail (Fréchet)	$\xi_s$	2.54	$\log(p_{90}/p_{50})$ wage	PSZ/DINA (2022)
Ability tail (Fréchet)	$\xi_z$	4.00	Gini business income	PSZ/DINA (2022)
Tax progressivity	$\tau_L$	0.079	ETR bottom 50%	DINA (2018)
Tax level	$\lambda_L$	0.778	ETR middle 40%	DINA (2018)
Home production	$c_0$	0.070	Participation elast.	<a href="#">Chetty (2012)</a>
<i>Statutory business tax</i>				
Bracket 1	$T_B$	0%	$d \leq \$50k$	IRC §1(h)
Bracket 2	$T_B$	15%	$\$50k-\$550k$	IRC §1(h)
Bracket 3	$T_B$	20%	$d > \$550k$	IRC §1(h)

# Calibration: moments

Moment	Model	Data	Identifies	Source
<i>Panel A: Targeted moments</i>				
Labor participation	0.672	0.620	$\kappa_1$	BLS (2022)
Entrepreneurship rate	0.093	0.100	$\kappa_2$	BLS CPS (2022)
Avg. employees per firm	9.29	10.00	$\alpha$	U.S. Census (2021)
CV of business income	1.33	1.20	$\sigma_\varepsilon$	<a href="#">DeBacker et al. (2021)</a>
$\log(p_{90}/p_{50})$ wage	0.987	0.997	$\xi_s$	PSZ/DINA (2022)
Gini of business income	0.632	0.650	$\xi_z$	PSZ/DINA (2022)
ETR bottom 50%	0.148	0.148	$\tau_L$	DINA (2018)
ETR middle 40%	0.213	0.214	$\lambda_L$	DINA (2018)
Participation elasticity	0.250	0.250	$c_0$	<a href="#">Chetty (2012)</a>
<i>Panel B: Untargeted moments</i>				
Inactivity rate	0.328	0.380	—	BLS (2022)
Wage Gini	0.342	0.520	—	PSZ/DINA (2019)
ETR top 10%	0.158	0.249	—	DINA (2018)
Avg. ETR labor	0.208	0.234	—	DINA (2018)
Top 10% wage share	0.279	0.375	—	PSZ/DINA (2019)
Top 10% business share	0.426	0.675	—	PSZ/DINA (2019)
Business income share	0.394	0.280	—	PSZ/DINA (2019)

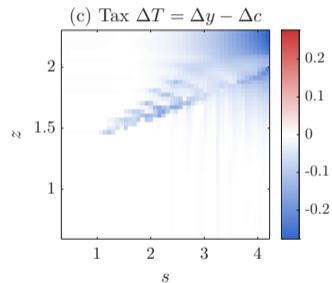
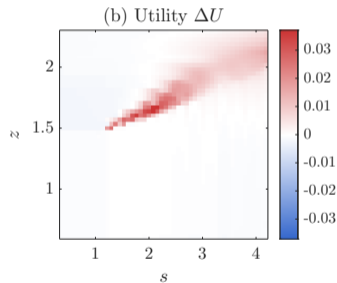
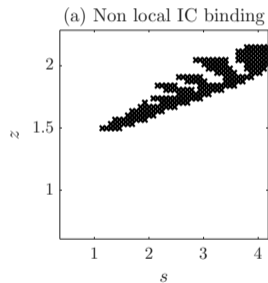
# Main quantitative result: localized tax breaks

**Message.** Tax breaks are concentrated near the occupational frontier.



# Global IC constraints matter locally

**Message.** Global IC matters most where cross-occupation deviations are tempting.



# Role of entrepreneurial risk

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Entrepreneurial risk affects optimal taxes through two channels.

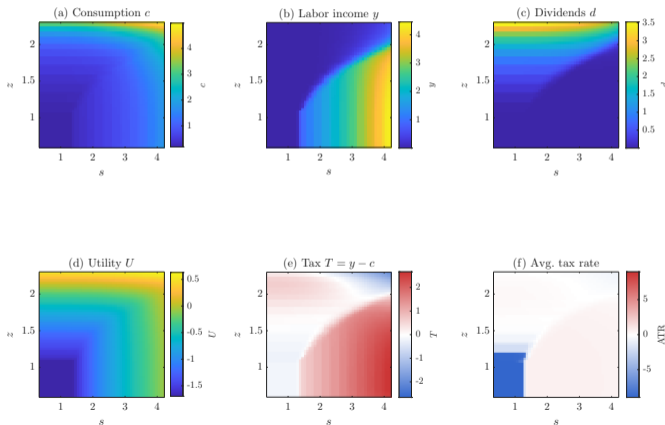
1. **Insurance.** Risk-averse agents value smoother consumption across profit realizations.
2. **Screening.** Taxes that depend on realized dividends can relax ex-ante incentive constraints.

## Benchmark contrast

Without risk, there is no shock-contingent insurance or screening. The planner relies more directly on occupational-entry incentives.

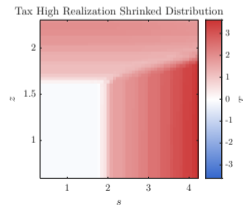
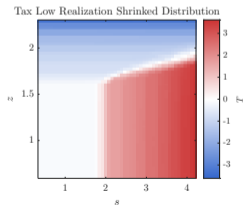
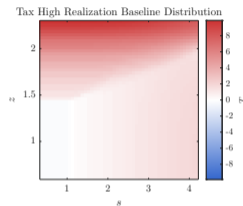
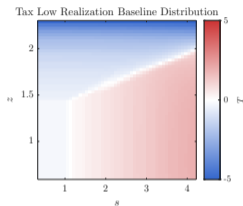
# No entrepreneurial risk

**Message.** Removing risk makes the entry-margin force more visible because taxes cannot use shock-contingent screening.



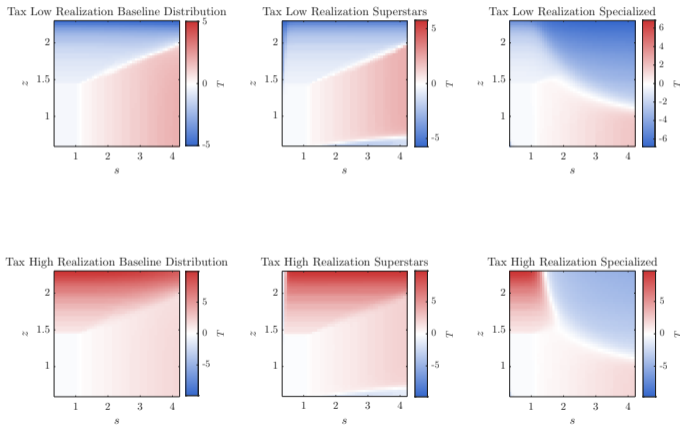
# Scarcity of high- $z$ entrepreneurs

**Message.** When high-ability entrepreneurs are scarce, sustaining entry becomes more valuable.



# Affiliation: superstars versus specialized talent

**Message.** Subsidies depend on the correlation between labor skill and entrepreneurial ability.



# Conclusion

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- ▶ Multidimensional private information creates an entry-margin motive for entrepreneurial tax breaks.
- ▶ General equilibrium amplifies this motive because entry supports labor demand.
- ▶ The lottery LP makes the full global-IC problem computationally tractable despite non-convexities.
- ▶ Quantitatively, the relevant distortions are highly localized near the entrepreneurship frontier.

**Backup slides**

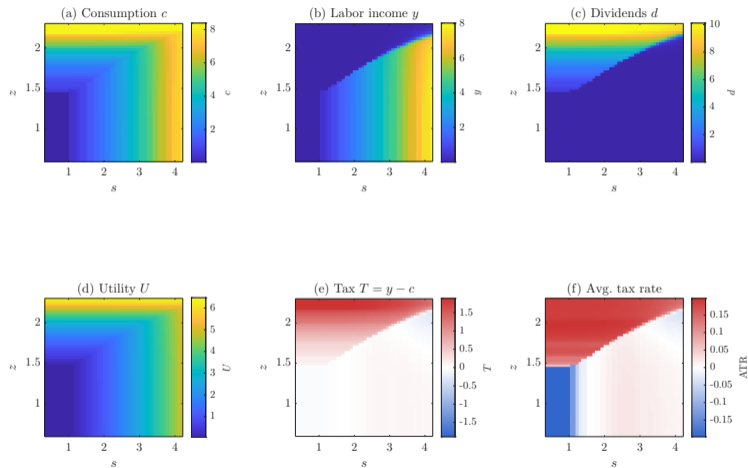
## Backup: full LP in compact form

$$\max_{\lambda, \mu} \sum_i \omega_i W_i \sum_r p_r \left[ \sum_k \lambda_{i,k,r} U_k - \sum_{(a,b) \in \mathcal{J}} \mu_{i,a,b,r} \mathcal{V}_{i,a,b,r} \right]$$

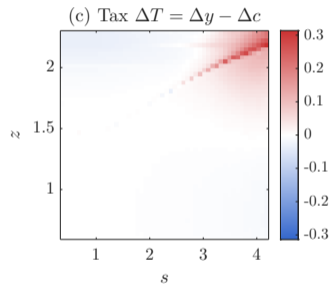
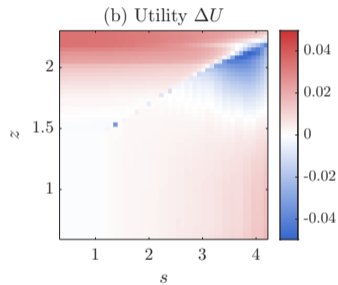
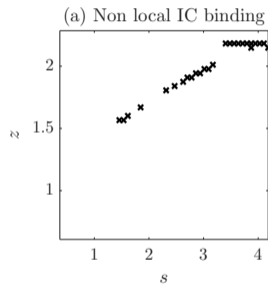
subject to simplex constraints, resource feasibility, labor-market clearing, IR, no shock-contingent occupational switching, and

$$\sum_r p_r \left[ \sum_k \lambda_{i,k,r} U_k - \sum_{(a,b) \in \mathcal{J}} \mu_{i,a,b,r} \mathcal{V}_{i,a,b,r} \right] \geq \sum_r p_r \left[ \sum_k \lambda_{j,k,r} U_k - \sum_{(a,b) \in \mathcal{J}} \mu_{j,a,b,r} \mathcal{V}_{i,a,b,r} \right].$$

# Backup: quasi-linear utility



# Backup: global IC with quasi-linear utility



## References

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- Chetty, R. (2012). Bounds on elasticities with optimization frictions: A synthesis of micro and macro evidence on labor supply. *Econometrica*, 80(3):969–1018.
- DeBacker, J., Heim, B. T., Panousi, V., Ramnath, S., and Vidangos, I. (2021). The distribution of business income: Evidence from pass-through entities. *National Tax Journal*, 74(4):911–938.